## The Central Limit Theorem (Section 9.2)

**The Central Limit Theorem**. Provided the conditions below are met (large sample or population distribution is normal) then *the distribution of sample means will be approximately normal.* 

Conditions that must be met for Central Limit Theorem to apply (page 416):

1. **Random and Independent.** The sample must be random and the observations in the sample must be independent from one another.

## 2. Large Sample or Normal Pop.

Either the sample size is "large"  $(n \ge 25)$ 

**OR** if you have a "small" sample, then you have to check or assume the underlying <u>population</u> is Normal

## Features of the Sampling Distribution of the Sample Means:

The mean of all the sample means is the same as the population mean.

 $\mu_{\bar{x}} = \mu$  (The mean of the means is the mean...ay yai yai! But easy in practice!)

The standard deviation of the all the sample means is called the "Standard Error"

$$\sigma_{\bar{x}} = SE = \sigma / \sqrt{n}$$

The z-score for an observed Sample Mean,  $\overline{X}$ , is found the usual way:  $z = \frac{observed - center}{SD}$ 

In this context, this is the formula: 
$$z = \frac{\overline{x} - \mu}{SE}$$

Sampling Distribution of 
$$\overline{x}$$



**Example:** Air Pollution and Children's Health. One of the measurements used to determine the health of a person's lungs is the <u>amount</u> of air a person can exhale under force in one second. This is called the "forced expiratory volume in one second" and is abbreviated  $FEV_1$ . Previous studies have established that the mean  $FEV_1$  for 10-year-old boys is 2.10 liters and that the population standard deviation is 0.3 liters. A random sample of 100 10-year-old boys who live in a community with high levels of ozone pollution is found to have a mean  $FEV_1$  of 1.95 liters.

What is the probability that the sample of boys in the polluted of areas would have a mean of 2.02 liters (or less) if the true population average for boys in polluted areas was actually 2.10 liters?

What do we know? (Parking Lot)

What do we want to find out?

Strategy: To find the probability we'll use the

First, we have to check that the conditions are met by this problem.

Check conditions for CLT:

Graph the Sampling Distribution for the mean. Sketch the z-axis under the  $\overline{x}$  - axis Shade the area that represents the probability. Find the the z-score and the probability



If this were a hypothesis test, what would we call this probability?

## **Types of significance:**

"Evidence-based practice requires clinicians to stay current with the scientific literature. Unfortunately, rehabilitation professionals are often faced with research literature that is difficult to interpret clinically. Clinical research data is often analyzed with traditional statistical probability (p-values), which may not give rehabilitation professionals enough information to make clinical decisions. **Statistically significant** differences or outcomes simply address whether to accept or reject a null or directional hypothesis, without providing information on the magnitude or direction of the difference (treatment effect). To improve the interpretation of **clinical significance** in the rehabilitation literature, researchers commonly include more clinically-relevant information such as confidence intervals and effect sizes. ... Understanding these aspects of research will help practitioners better utilize the evidence to improve their clinical decision-making skills."

• Statistical significance: This is based on an <u>inference</u> made by using a hypothesis test.

Did the kids in the high pollution areas have statistically significant reduction in lung function? Explain.

• **Clinical significance:** This is determined by experts in health and mental health fields. A <u>statistically</u> <u>significant</u> effect may or may not be <u>clinically significant</u>!

In the context of the air pollution problem above, do we know how much of a reduction in  $FEV_1$  is *clinically significant*? Explain.

• **Practical significance:** This is determined based on the context of the research and what matters in that situation. Again, a *statistically significant* finding may or may not be *practically significant*!

Climate data shows there has been an increase of average ocean temperatures of 1 degree Fahrenheit over the last century. Is this small change in temperature of any *practical significance*?